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Polymer class specificity of the glass temperature

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Abstract

It is shown that assuming linearity of the polymer class specific correlation between the glass transition temperature and the ratio mass to effective number of 'flexible' bonds of monomeric (repeat) unit, μ/ρ , it is possible to evaluate by least square fit the 'flexibility' factor, ρ , characterizing the share of those simple bonds within the repeat unit responsible for conformational rearrangements of the polymer. The evaluated effective number of simple bonds accounts for the influence of polymer class specific interactions and steric hindrances on the 'free rotation' of the simple bonds comprised in the repeat unit. It is shown that the well-known increase of the glass transition temperature of polymers bearing longer n-alkylic side chains may be the result of preferred 'crankshaft' like motions of neighboring methylenes, hindering the 'free rotation' of the simple bonds between the methylenes involved in the 'crankshaft'. It is also possible to quantify steric hindrances of bulky substituents.

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1. Introduction

The glass transition is a distinguishing mark of polymeric materials showing the characteristics of a second-order thermodynamic transition (e.g. continuity of volume, enthalpy and other first order derivatives of the Gibbs free energy, but discontinuity of the second order derivatives, i.e. expansion coefficient, heat capacity, etc.) [\[1\].](#page-7-0) However, the experimentally observed frequency and time dependence points to the fact that the transition does not occur under thermodynamic equilibrium condition, the polymer being 'frozen-in'. Accordingly polymeric glasses show relaxation phenomena which depend on 'relaxation entropy' and 'free volume', being controlled by the tendency of the 'metastable' glass to approach thermodynamic equilibrium ('aging' of polymers). Thus two main models have been developed for the theoretical description of the glass transition phenomenon: the kinetic based 'free volume' and the thermodynamic based 'conformational entropy' theory.

The kinetic theory assumes that the mobility of molecules is controlled by the 'free volume' and the glass transition occurs as soon as the temperature dependent decrease of the free volume within the amorphous phase reaches some characteristic value preventing any further molecular rearrangements [\[2\]](#page-7-0).

According to the thermodynamic theory the glass is considered a fourth state of matter, characterized by 'zero-conformational' entropy which can be evaluated in terms of an 'S-V-T' equation of state [\[3\]](#page-7-0). The transition to the thermodynamic stable glass is characterized in this state diagram by a second-order transition temperature, T_2 , situated about 50 K below the experimentally observable glass temperature, $T_{\rm g}$. Conformational changes contributing to the conformational entropy are controlled by 'flexible bonds', i.e. those simple bonds which by rotation allow conformational changes of the molecule.

Unfortunately there is no way to verify experimentally the validity of any of these two theories. Because of the kinetic dependent 'freeze-in' phenomenon of the glass transition, the calculated second-order transition, T_2 , is experimentally not accessible, whereas the estimated values

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of 'free volume' differ, depending on the definition used, by several orders of magnitude [\[4\]](#page-7-0).

Besides the molecular weight (through 'chain end effects') and the degree of crosslinking [\[5\]](#page-7-0) the glass transition temperature of polymers depends on a series of molecular parameters, the prevailing two factors being the chain flexibility related to the characteristic ratio [\[6\]](#page-7-0) and the inter/intramolecular interactions characterized by the cohesive energy density [\[7\]](#page-7-0).

The chain flexibility is first of all controlled by the barrier to rotation of the backbone C–C bonds. The larger the substituent and the stronger the interaction between substituents the more hindered will be this rotation. Additionally the hindrance to rotation is accentuated by multiple anchoring on the same C (two or three substituents) increasing the glass transition temperature.

On the other hand longer n -alkylic side chains lower the glass transition temperature due to an internal 'plasticizing effect' of the main chain. Natta et al. [\[8\]](#page-7-0) have shown already in 1957 the plasticizing effect of short *n*-alkylic side chains on the glass transition temperature of $poly(\alpha$ -olefin)s.

Taking into account both the theoretical and technological importance of knowing the glass transition of polymers, several semiempirical methods have been suggested in literature for predicting T_g . One of these methods scales the volume contributions to T_g of the different chemical constituents of the repeating unit [\[9\].](#page-7-0) Hopfinger et al. [\[10\]](#page-7-0) have developed a model to estimate $T_{\rm g}$ using conformational flexibility and mass moments, assuming group additivity and correlating by least square fit the calculated values with experimental T_g -data. The model has subsequently been extended to account for intermolecular contributions [\[11\]](#page-7-0).

Schneider and DiMarzio [\[12\]](#page-7-0) suggested the more simple correlation of T_g with the mass per 'flexible' bond of the monomeric (repeat) unit

$$
T_{\rm g} = A + C(\mu/\rho) \tag{1}
$$

with μ the mass and ρ the number of 'flexible' bonds of the monomeric unit. A and C are polymer class specific constants being associated with the very similar interactions and hindrances within a given class of polymers [\[13\]](#page-7-0). The prevailing problem of this correlation is related to the exact counting of the effective number of 'flexible' bonds contributing by rotation to conformational changes of the repeat unit because of unknown hindrances due to inter/ intramolecular interactions and steric effects. Nevertheless the scatter of the data is not larger than for the other proposed semiempirical correlations [\[13,14\]](#page-7-0).

2. Dependence of the glass temperature on the length of *n*-alkylic side chain and the bulkiness of substituents

In order to show the influence of the length of n alkylic side chains and of the bulkiness of substituents on the glass transition temperature of polymers, $T_{\rm g}$, data were taken from the 'Polymer Handbook' [\[15\]](#page-7-0) for five classes of polymers. They are presented in [Table 1](#page-2-0). Taking into account the very conflicting data in the literature for poly(ethylene) the value of Boyer [\[16\]](#page-7-0) has been used in the following discussion.

2.1. Influence of the bulkiness of the side-group of monosubstituted polymers

It is known that the glass transition temperature of monosubstituted polymers increases with the bulkiness of the substituent. It is, however, surprising that the increase of the glass transition temperature of $poly(\alpha$ -olefin)s seems to be directly proportional to the atomic mass of the substituents. For the other classes of polymers studied this general tendency of T_g -increase to the atomic mass of the substituent is confirmed, but the scatter of the data is, however, much larger (see signs with question-marks in Fig. 1).

For instance, the glass transition temperatures of all other iso-propyl substituted polymers are much smaller than expected from the atomic mass of the substituent. The observed higher T_g -values of the poly(phenyl acrylic/methacrylic ester)s compared to those of the heavier poly(cyclohexyl ester)s may be explained by additional hindrances of the free rotation of the

Fig. 1. Dependence of the glass transition temperature on the atomic mass of substituents. PE, poly(ethylene)s; PS, poly(styrene)s; PMetAc, poly- (methacrylic ester)s; PAcr, poly(acrylic ester)s; PB, poly(butadiene)s lines by linear fit (symbols with crosses being neglected).

Table 1 (continued)

^a Number of methylenes between main chain and end-methyl group of the *n*-alkylic side chain.

^b T_g -data taken from Peyser [\[15\].](#page-7-0)

^c Mass/'flexible' bond of repeat (monomeric) unit.

^d All simple bonds, exept of

Possible 'crankshaft' movements of at least 4 neighboring methylenes will hinder the free rotation of the simple bonds between the methylens involved in the 'crankshaft'.

f Conflicting interpretation of PE T_g data, see [\[15\]](#page-7-0).
^g T_g -data of Boyer [\[16\]](#page-7-0).
^h Multiple anchoring of methyls to the same C-atom will hinder their free rotation.

ⁱ For cyclohexane are considered the two possible conformations.

^j The stiff phenyl ring may be arranged in or out of the main-chain plane, additionally it may be stiffened in esters by $\pi-\pi$ interaction with the free electrons of the oxigen of the acidic group, or with the adjacent phenyl of PS and the double bonds of polydiene, respectively.

k Possible hydrogen bonding reduces the 'flexibility' of the free acidic group.
 $\frac{1}{1}$ Substitution of the acidic hydrogen will liberate the flexibility of $\text{-COO}-$ in polyesters.

m Favoured 'crankshaft' motion of the backbone of the repeat units increases the 'flexibility' of cis-butadiene compared to trans-butadiene, where 'crankshaft' arrangements of the repeat units are structurally less probable.

phenyl-ring caused by $\pi-\pi$ interactions of the phenyl with the free electrons of the oxygen of the acidic – COO– group, and in poly(4-phenyl-styrene) by the $\pi-\pi$ interaction with the neighboring phenyl of polystyrene, respectively.

2.2. Influence of the length of the n-alkylic side chain on T_o

As mentioned before, the experimentally observed decrease of the glass transition temperature of $poly(\alpha$ olefin)s with the length of the n -alkylic side chain has been

Fig. 2. Dependence of the glass transition temperature on the length of the n-alkylic side chain bearing methyl end-groups; lines by third order fit.

attributed to an internal 'plasticizing effect' [\[8\]](#page-7-0). The data exhibited in Fig. 2 show that this 'plasticizing effect' is general for all classes of polymers studied, but the T_{g} lowering effect ends for polymers with the longer n-alkylic side chains. T_g increases anew for the polymers bearing longer *n*-alkylic side chains. The glass transition temperatures show a minimum at the n -hexyl/ n -octyl derivatives of the more flexible main chains [i.e. $poly(\alpha$ -olefin)s, poly- $(n-alky)$ acrylate)s and poly $(n-alky)$ butadiene)s] and at noctyl/n-decyl for the derivatives of the stiffer poly(n-alkyl) methylacrylate)s and poly(4-n-alkyl styrene)s, respectively.

Side chain crystallization is the explanation usually invoked in the literature to account for the observed increase of T_g of the higher *n*-alkylic side chain polymers. According to this assumption, side chain crystallization leads to a denser packing of the polymer accompanied by a corresponding decrease of the 'free volume' and thus by an increase of T_{σ} .

A second possible explanation which will be presented in the following starts with the supposition that possible 'crankshaft' like motions of at least 4 adjacent methylenes within the n-alkylic side chain reduces the effective 'flexibility' of $-CH_2-CH_2$ - simple bonds involved in the 'crankshaft', reducing thus the overall 'flexibility' of the repeat unit. This assumption is supported by the T_{σ} data shown for the poly(*n*-alkyl ethylene)s in Fig. $3(A)$.

This 'crankshaft' like motions of groups of 4 neighboring methylenes will hinder the 'free rotation' of the within involved individual $-CH_2-CH_2-$ simple bonds reducing

Mass/'flexible' bond ratio of monomeric unit

Fig. 3. (A) Dependence of the glass transition temperature of $poly(n-alky)$ ethylene)s on the mass/'flexible' bond ratio of monomeric unit open squares—all simple bonds are counted as 'flexible' bonds contributing by 'free rotation' to conformational rearrangements; line by third order fit open circles—hindering effect of 'crankshaft' like motions of at least four neighboring methylenes on the 'free rotation' of the methylenes of the 'crankshaft'; line by linear fit. (B) Dependence of the glass transition temperature of poly(ethylene)s on the 'flexibility' (mass/'flexible' bonds ratio) of the monomeric unit accounting for hindrances by 'crankshaft' like motions and steric effects of bulky alkylic/arylic substituents, respectively open signs: n-alkylic side-chain derivatives; signs with crosses: bulky alkylic/arylic substituents; line by linear fit.

 (A)

consequently the effective number of 'flexible' bonds compared to the overall number of simple bonds of the nalkylic side chain as shown in [Table 1](#page-2-0). (Compare columns 'simple' and 'crankshaft' of the heading μ/ρ). In accordance with the Schneider–DiMarzio rule (Eq. (1)), the result of this assumption is supported by the linearity of the corresponding T_g vs. μ/ρ data (shown by circles). Counting, on the contrary, all simple bonds within the n -alkylic side chain as 'flexible' bonds the respective data (squares) show a minimum. Unfortunately, the determination of the exact number of 'flexible' bonds, assuming hindrances by 'crankshaft' motions is only possible by a least squares fit to a straight line of the T_g vs. μ/ρ correlation. It is interesting to note that extrapolation of the resulting linear $T_{\rm g}$ vs. μ/ρ correlation of poly(*n*-alkyl ethylene)s confirms the T_g value of Boyer [\[16\]](#page-7-0) for 'amorphous' poly(ethylene) deduced by extrapolation of poly(ethylene) T_g -data for zero crystallinity.

In [Fig. 3\(](#page-4-0)B) are shown the glass transition temperatures of all poly(olefin)s listed in [Table 1,](#page-2-0) as well as those of poly(alkyl/aryl ethylene)s (symbolized by crosses) to evidence in addition the effect of the bulkiness of the different substituents on the overall 'flexibility' of the respective monomeric units. It is worth mentioning that the linearity correlation factor of $R=0.984$ is astonishingly good. B is the slope of the linear T_g vs. μ/ρ correlation.

Using the same procedure we obtained similarly satisfactory linear T_g vs. μ/ρ correlations for all other polymers listed in [Table 1](#page-2-0) bearing n-alkylic side chains and alkyl/arylic bulky substituents, respectively. The resulting correlation factors, R , and the slopes of the obtained straight lines, B , are shown in the respective plots; in Fig. $4(A)$ for poly(acrylic/methacrylic ester)s and in Fig. 4(B) for poly(4 alkyl/aryl styrene)s and poly(1-alkyl/aryl-1-butylene)s, i.e. poly(diene)s.

The correlation factors, R , and the belonging slopes, B , of the T_g vs. μ/ρ straight lines of the analyzed polymer classes bearing n -alkylic side chains (including derivatives with bulky alkyl/arylic substituents) are listed in [Table 2.](#page-6-0) It is interesting to mention that the values of the correlation factors are surprisingly good taking into account the fit method used to evaluate the effective number of 'flexible' bonds of the n-alkylic side chain derivatives. The different slopes of the T_g vs. μ/ρ correlations of the studied polymer classes support the assumption that similar interactions and hindrances are acting within a given class of polymers.

It is, however, unexpected that the slopes of the T_g vs. μ/ρ linear correlations increase with the decrease of the 'flexibility' of the repeat units. This is reflected in the generally higher T_g -values of the same derivatives of the studied polymers. In [Table 2](#page-6-0) are listed for comparison the T_g values of the respective methyl derivatives.

Finally in Fig. $5(A)$ are shown the 'flexibility' factors, ρ , deduced by the least square fit procedure used to draw the respective T_g vs. μ/ρ linear correlations of the different classes of polymers bearing n-alkylic side chains. For better

Glass Transition Temperatures of 500 Poly(acrylic/methacrylic ester)s Glass Transition Temperature, K
Class Transition Temperature, K
250
Class Tomperature m O Poly(alkyl/aryl acrylic esters) Δ Poly(alkyl/aryl methacrylic esters) 200 The numerals indicat the number of side chain C-atoms of the Poly(n-alkyl acrylic/methacrylic a 20 25 30 35 40 Mass/'flexible' bond ratio of monomeric unit (B) 450 **Glass TransitionTemperatures** of Poly(styrene)s and Poly(diene)s 400 \times Glass Transition Temperature, 350 ethyl (2) 300 250 200 Poly(4-alkyl/aryl styrenes) Poly(1-alkyl/aryl-1-butylene)s Poly(butadiene)s rals indicat the number of C-ato 150 of the 4-/1-n-alkylic side chain 20 25 30 35 15 Mass/'flexible' bond ratio of monomeric unit

Fig. 4. (A) Dependence of the glass transition temperature of poly(acrylic-) and poly(methacrylic ester)s on the 'flexibility' of the monomeric unit accounting for possible 'crankshaft' like and steric hindrances. For significance of open and crossed symbols, see [Fig. 3](#page-4-0)(B); lines by linear fit. (B) Dependence of the glass transition temperature of poly(styrene)s and poly(butadiene)s on the 'flexibility' of the monomeric unit accounting for possible 'crankshaft' like and steric hindrances. For significance of open and crossed signs, see [Fig. 3\(](#page-4-0)B); lines by linear fit.

Table 2 Correlation factors and slopes of the T_g vs. μ/ρ straight lines

Polymer class	R corr f	B slope	T_{φ} , K of methyl derivatives
$Poly(1-n-alkyl-1-$ butylene)s	0.987	10.12	$206 - 218$
$Poly(n-alkyl-ethyl-$ ene)s	0.984	11.38	258-270
$Poly(n-alkyl-acrylic)$ ester)s	0.984	13.28	283
$Poly(n-alkyl-)$ methacrylic ester)s	0.971	15.97	378
Poly $(4-n-alkyl$ styr- ene)s	0.980	16.90	375

comparison in Fig. 5(B) are presented normalized 'flexiflexibility' factors evaluated as differences between the 'flexibility' factors of the various n-alkylic side chain derivatives and the respective methyl derivative. Except for the higher *n*-alkyl derivatives of the poly $(n$ -alkyl acrylic ester)s the agreement between the 'normalized' flexibility factors of the different classes of polymers is amazingly good. This is confirmed by the correlation factor of $R=$ 0.998 of the accepted third order fitting equation. This proves that the hindering effect of crankshaft motions of at least four neighboring side chain methylenes on the 'free rotation' of simple bonds between the methylenes included in the crankshaft is the same, irrespective of the nature of the polymeric backbone.

It is interesting to notice that cooperative trans–gauche 'crankshaft' like motions in poly(ethylene) have been involved to explain the experimentally observed different characteristic 'freeze-in' processes of poly(ethylene) showing distinct T_g values [\[17,18\].](#page-7-0)

The same procedure to evaluate 'normalized' flexibility factors was used for derivatives bearing bulky substituents. This showed that the diverse classes of polymers studied have different linear correlations suggesting specific interactions between the polymeric backbone and the bulky substituents. (see [Fig. 6\)](#page-7-0). So, for instance, the derivatives with bulky substituents of poly(acrylic-) and poly(methacrylic ester)s show the same 'normalized' flexibility factors, differing from those of the derivatives of poly(ethylene)/poly(styrene) and poly(butadiene), respectively.

3. Conclusions

Least square fits were used to evaluate 'flexibility' factors, ρ , from the linear correlation between the glass transition temperature and the mass/'flexible' bond ratio of the monomeric unit $(T_{\rm g}$ vs. μ/ρ). The 'flexibility' factors account for polymer class specific interactions and steric hindrances on the 'free' rotation of those simple bonds responsible for conformational rearrangements. Applying

Fig. 5. (A) Dependence of the 'flexibility' factor of *n*-alkylic side chains derivatives on the number of methylens to the methyl end-group evidencing the hindering effect of 'crankshaft' like motions on the 'free rotation' of simple bonds; lines by third order fit. (B) Dependence of the normalized 'flexibility' factor of n-alkylic side chains on the number of methylenes to the methyl end-group; line by third order fit.

Fig. 6. Dependence of the normalized 'flexibility' factor on the atomic mass of bulky substituents connected directly to the basic monomeric unit. For significance of the symbols see [Fig. 5\(](#page-6-0)B).

this procedure it is shown that the experimentally observed renewed increase of the glass transition temperature of polymers bearing longer n-alkylic side chains may by explained not only by the typically assumed, but in our opinion less probable side chain crystallization, but also by supposing 'crankshaft' like motions of at least four neighboring methylenes which will hinder the 'free' rotation of the simple bonds between the methylenes involved in the 'crankshaft' structure.

We would also like to point out that the normalized 'flexibility' factors deduced by fits and expressed by the difference between the respective 'flexibility' factors, of the longer n-alkylic side chains and the corresponding methylic derivatives are the same for the different classes of polymers studied, although generally the T_g vs. μ/ρ behavior is polymer specific. However, the polymer class specificity is reflected by both the overall T_g vs. μ/ρ behavior of the analyzed polymer classes as well by the normalized 'flexibility' factors of the different bulky substituents.

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